

Cambridge Assessment International Education

Cambridge International General Certificate of Secondary Education

ADDITIONAL MATHEMATICS

0606/12

Paper 1 May/June 2019

MARK SCHEME
Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

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This document consists of 11 printed pages.



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Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always whole marks (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit
 is given for valid answers which go beyond the scope of the syllabus and mark scheme,
 referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these
 features are specifically assessed by the question as indicated by the mark scheme. The
 meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

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MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- M Method marks, awarded for a valid method applied to the problem.
- Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy Α marks to be given, the associated Method mark must be earned or implied.
- В Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

answers which round to awrt correct answer only cao

dep dependent

follow through after error FT ignore subsequent working isw nfww not from wrong working

or equivalent oe

rounded or truncated rot

Special Case SC seen or implied soi

Question	Answer	Marks	Guidance
1(a)		B1	
		B1	

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Question	Answer	Marks	Guidance
1(b)	$P = \{30^{\circ}, 150^{\circ}, 210^{\circ}, 330^{\circ}\}$	B1	May be seen or implied in a Venn diagram Allow without set notation
	$Q = \{30^{\circ}, 150^{\circ}\}$	B1	May be seen or implied in a Venn diagram Allow without set notation
	$P \cap Q = \{30^{\circ}, 150^{\circ}\}$	B1	Dep on both previous B marks Must be in set notation
2	Either: $(2x+3)^2(x-1) = 3(2x+3)$ $(2x+3)(2x^2+x-6)(=0)$	M1	For attempt to equate line and curve and attempt to simplify to $2x+3 \times a$ quadratic factor or cancelling $2x+3$ and obtaining a quadratic factor
	$(2x+3)(2x^2+x-6) = 0$ $(2x+3)(2x-3)(x+2) = 0$	M1	Dep for attempt at 3 linear factors from a linear term and a quadratic term
	$\left(-\frac{3}{2},0\right)$	B1	
	$\left(\frac{3}{2},18\right)$	A1	Dep on first M mark only
	(-2, -3)	A1	Dep on first M mark only
	Or: $(2x+3)^2(x-1) = 3(2x+3)$ $4x^3 + 8x^2 - 9x - 18(=0)$	M1	For attempt to equate line and curve and attempt to simplify to a cubic equation, by collecting like terms
	$(x+2)(4x^{2}-9)$ $(2x-3)(2x^{2}+7x+6)$ $(2x+3)(2x^{2}+x-6)$ $(2x+3)(2x-3)(x+2)(=0)$	M1	Dep For attempt to find a factor from a 4 term cubic equation (usually $x+2$), do long division oe to obtain a quadratic factor and factorise this quadratic factor
	$\left(-\frac{3}{2},0\right)$	A1	
	$\left(\frac{3}{2},18\right)$	A1	
	(-2, -3)	A1	
3(i)	1000	B1	

Question	Answer	Marks	Guidance
3(ii)	$\frac{dB}{dt} = 400e^{2t} - 1600e^{-2t}$	B1	
	$3 = e^{2t} - 4e^{-2t}$ oe	M1	For equating an equation of the form $ae^{2t} + be^{-2t}$ to 1200 and dividing by 400
	$e^{4t} - 3e^{2t} - 4 = 0$	A1	
3(iii)	$(e^{2t} + 1)(e^{2t} - 4) = 0$	M1	For attempt to factorise and solve, dealing with exponential correctly, to obtain $e^{2t} =$
	$t = \ln 2$, $\frac{1}{2} \ln 4$ or awrt 0.693 only isw if appropriate	A1	
4(a)	$a = \frac{5}{2}$	B1	
	$b = -\frac{3}{2}$	B1	
	$c = \frac{11}{2}$	B1	
4(b)	$9x^{\frac{1}{2}} - 3y^{-\frac{1}{2}} = 12$ $4x^{\frac{1}{2}} + 3y^{-\frac{1}{2}} = 14$	M1	For attempt to solve simultaneous equations. Must reach $kx^{\frac{1}{2}} =$ or $ky^{-\frac{1}{2}} =$ oe
	x = 4	A1	
	$y = \frac{1}{4}$	A1	
5(i)	$9.6 = 12\theta$	M1	For use of arc length
	$\theta = 0.8$	A1	

Question	Answer	Marks	Guidance
5(ii)	Either $\tan \theta = \frac{AB}{12}, (AB = 12.36)$ Or $OB = \frac{12}{\cos \theta} (OB = 17.22)$	M1	For attempt to find AB or OB using their θ May be implied by a correct triangle area Allow if using degrees consistently
	Either $Area \Delta OAB = \frac{1}{2} \times 12 \times their \ 12.36$ Or $Area \Delta OAB = \frac{1}{2} \times 12 \times their \ 17.22 \times sin\theta$ $(= 74.1 \text{ or } 74.2)$	M1	Allow if using degrees consistently
	Area of sector $OAC = \frac{1}{2} \times 12^2 \times 0.8$ = 57.6	B1	Allow unsimplified
	Area of shaded region = 16.5 or 16.6	A1	
6(a)(i)	40320	B1	
6(a)(ii)	No. of ways with maths books as 1 unit = 5! or $5 \times 4!$ or 5P_5 or 120	B1	
	No. of ways maths books can be arranged amongst themselves = $4!$ or 4P_4 or 24	B1	
	Total = $(5! \times 4! \text{ oe}) = 2880$	B1	
6(a)(iii)	No. of ways with maths books as 1 unit and geography books as 1 unit = $3!$ or 3P_3 or $3 \times 2!$ or 6	B1	
	No. of ways maths books can be arranged amongst themselves and geography books can be arranged amongst themselves = $4! \times 3!$ or ${}^4P_4 \times {}^3P_3$ or 144	B1	
	Total = $(3! \times 4! \times 3! \text{ oe})$ = 864	B1	
6(b)(i)	$^{12}C_6 = 924$	B1	

Question	Answer	Marks	Guidance
6(b)(ii)	Either: 924 – ⁸ C ₆	M1	For <i>their</i> (i) – the number of teams of just men
	Total = 896	A1	
	Or: $5M \ 1W : {}^{8}C_{5} \times {}^{4}C_{1} (=224)$ $4M \ 2W : {}^{8}C_{4} \times {}^{4}C_{2} (=420)$ $3M \ 3W : {}^{8}C_{3} \times {}^{4}C_{3} (=224)$ $2M \ 4W : {}^{8}C_{2} \times {}^{4}C_{4} (=28)$	M1	For a complete method
	Total = 896	A1	
7(i)	$ \begin{array}{c c} 120 \\ \hline \beta & 35 \end{array} $ $ \begin{array}{c c} \alpha \end{array} $	B1	For correct triangle, may be implied by a correct sine rule or cosine rule.
	$\frac{120}{\sin \alpha}$ or $\frac{120}{\sin(55-\theta)} = \frac{650}{\sin 35}$ or $\frac{650}{\sin 145}$	M1	For use of a correct sine rule to obtain $\alpha =$ or $\theta =$ Or for a correct cosine rule leading to a value for v , followed by a correct sine rule leading to one of the other angles
	$\alpha = 6.08^{\circ} \text{ or } \beta = 138.9$	A1	May be implied by a correct $\theta = \text{awrt } 49^{\circ}$
	Bearing is 048.9° or 049°	A1	
7(ii)	Either $\frac{v_r}{\sin(145 - their\alpha)} = \frac{650}{\sin 35} \text{ or } \frac{120}{\sin(their\alpha)}$ Or $v_r^2 = 650^2 + 120^2 - (2 \times 650 \times 120)\cos(145 - their\alpha)$	M1	For use of sine rule or cosine rule to find resultant velocity Do not allow for a right-angled triangle May be seen in (i)
	$v_r = 745$	A1	For correct resultant velocity, allow awrt 745
	Time taken = $\frac{1250}{their 744.7}$	M1	For correct attempt at finding time using <i>their</i> v , \neq 650, 120, 770 or 530
	=1.68 hours or I hour 41 mins or 101 mins	A1	

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Question	Answer	Marks	Guidance
8(i)	$e^{y} = \frac{m}{x} + c$	B1	May be implied by subsequent work
	Either $20 = 2m + c$ 8 = 4m + c	M1	For at least 1 correct equation
		M1	Dep For attempt to solve <i>their</i> 2 equations simultaneously to obtain at least one unknown
	leading to $m = -6$, $c = 32$	A1	For both
	$y = \ln\left(32 - \frac{6}{x}\right)$	A1	Must have correct brackets Mark the final answer given
	Or: Gradient = $m = (-6)$	M1	For attempt to find gradient and equate it to <i>m</i>
	$20 = 2m + c \text{ or } 8 = 4m + c$ or $e^y - 8 = m\left(\frac{1}{x} - 4\right)$ or $e^y - 20 = m\left(\frac{1}{x} - 2\right)$	M1	For at least 1 correct equation, may be using <i>their m</i>
	leading to $c = 32$ and $m = -6$	A1	For both $m = -6$, $c = 32$
	$y = \ln\left(32 - \frac{6}{x}\right)$	A1	
8(ii)	$x > \frac{3}{16}$ oe	B1	
8(iii)	$y = \ln 30$ isw	B1	
8(iv)	$2 = \ln\left(32 - \frac{6}{x}\right)$	M1	For a correct substitution and attempt to re-arrange using 2, <i>their</i> 32 and <i>their</i> – 6, keeping exactness to obtain $x =$
	$x = \frac{6}{32 - e^2}$ oe	A1	Must be exact

Question	Answer	Marks	Guidance
9(i)	$5 = 4 + 2\cos 3x$	M1	For attempt to solve trig equation to obtain one correct solution
	$\frac{\pi}{9}$	A1	
	$-\frac{\pi}{9}$	A1	
9(ii)	Either: $\int_{-\frac{\pi}{9}}^{\frac{\pi}{9}} 4 + 2\cos 3x - 5 dx$	M1	For use of subtraction method
	$\left[\frac{2}{3}\sin 3x - x\right]_{-\frac{\pi}{9}}^{\frac{\pi}{9}}$	M1	For attempt to integrate to obtain the form $a \sin 3x + bx$
		B1	For $\frac{2}{3}\sin 3x$
		B1	For $-x$, may be implied by $4x-5x$
	$\left(\frac{\sqrt{3}}{3} - \frac{\pi}{9}\right) - \left(-\frac{\sqrt{3}}{3} + \frac{\pi}{9}\right)$	M1	Dep on previous M mark for correct application of <i>their</i> limits in radians from (i) retaining exactness
	Shaded area = $\frac{2\sqrt{3}}{3} - \frac{2\pi}{9}$ oe isw	A1	

Question	Answer	Marks	Guidance
9(ii)	Or: Area of rectangle = $5 \times \frac{2\pi}{9}$	M1	5× the difference of <i>their</i> limits in exact radians
	Area under curve = $\left[4x + \frac{2}{3}\sin 3x\right]_{-\frac{\pi}{9}}^{\frac{\pi}{9}}$	M1	For attempt to integrate to obtain the form $a \sin 3x + bx$
		B1	For $\frac{2}{3}\sin 3x$
		B1	For 4x
	$\left(\frac{\sqrt{3}}{3} + \frac{4\pi}{9}\right) - \left(-\frac{\sqrt{3}}{3} - \frac{4\pi}{9}\right)$ $\left(=\frac{2\sqrt{3}}{3} + \frac{8\pi}{9}\right)$	M1	Dep on previous M mark for correct application of <i>their</i> limits in exact radians from (i) retaining exactness
	Shaded area = $\frac{2\sqrt{3}}{3} - \frac{2\pi}{9}$ oe isw	A1	
10(i)	$800 = 4x^2h$	B1	
	$h = \frac{800}{4x^2}$ oe or $xh = \frac{800}{4x}$ oe	B1	
	$(S=)2hx+8xh+4x^2 \text{ oe}$	M1	Allow if <i>h</i> is substituted at this point
	$S = 4x^2 + \left(\frac{2000}{x}\right)$	A1	Leading to AG, must have $S = \text{or}$ surface area = at some point and no errors

Question	Answer	Marks	Guidance
10(ii)	$\left(\frac{\mathrm{d}S}{\mathrm{d}x} = \right)8x - \frac{2000}{x^2}$	B1	For correct differentiation
	When $\frac{dS}{dx} = 0$, $x = \sqrt[3]{250}$ oe (6.30)	M1	For equating to zero and attempt to solve, must get as far as $x =$, must be using the form $ax + \frac{b}{x^2}$
		A1	For correct positive x
	S = 476 only	A1	
	$\frac{d^2S}{dx^2} = 8 + \frac{4000}{x^3}$ $\frac{d^2S}{dx^2} > 0 \text{ or } 24 \text{ so minimum}$	В1	For a correct convincing method, with enough detail to reach a correct conclusion of a minimum. Must be using $x = \sqrt[3]{250}$ oe
11		M1	For attempt at differentiating a product
		B1	For $\frac{2}{3} \times 3(3x+1)^{-\frac{1}{3}}$
	$\left(\frac{dy}{dx} = \right)(x-2) \times \frac{2}{3} \times 3(3x+1)^{-\frac{1}{3}} + (3x+1)^{\frac{2}{3}}$	A1	For all other terms correct
	$y = \frac{4}{3}$	B1	
	When $x = \frac{7}{3}$, $\frac{dy}{dx} = \frac{13}{3}$	M1	For attempt at normal equation using $-\frac{1}{their\ m}$ and their y when $x = \frac{7}{3}$
	Equation of normal: $y - \frac{4}{3} = -\frac{3}{13} \left(x - \frac{7}{3} \right)$	A1	For correct normal equation, may be implied by a correct final answer
	At y-axis, $y = \frac{73}{39}$ $\left(0, \frac{73}{39}\right) \text{ isw}$	A1	